- I sketch the graph of the binary sigmoidal function  $F(x) = \frac{1}{1 + e^{-x}}$
- Verify that: 0 < f(x) < 1 and f(-x) = 1 f(x) Calculate f(0), f(2), and f(-2).
- 2 Convince yourself that f(x), in Problem 1, is bounded, Continuous, monotonically increasing, and differentiable at all points.
- In problem.1, verify that x = ln [f(x)] ln [i f(x)]What is the value of x when f(x) = 0.75.7
- 4) verify that the derivative of f(x), in problem. 1, is

expressed as:  $\frac{df(x)}{dx} = \frac{e^{-x}}{(1+e^{-x})^2}$ 

or alternatively,  $\frac{df(x)}{dx} = f(x) \left[ 1 - f(x) \right]$ 

5) sketch the graph of  $\frac{df(x)}{dx}$ , in problem. 4 verify that this graph is symmetric about the X=0 axis, and that  $\frac{df(x)}{dx}$  has a maximum value of 0.25 at x=0, Calculate  $\frac{df(x)}{dx}$  and  $\frac{df(x)}{dx}$   $\frac{df(x)}{dx}$ 

For agiven value of  $\frac{df(x)}{dx}$ , in Problem 4, Verify that there are two values of x, XI and Xz, Such that

and  $f(x_1) + f(x_2) = 1$ 

Calculate  $x_1$ ,  $x_2$ ,  $f(x_1)$ , and  $f(x_2)$  when  $\frac{df(x)}{dx} = 0.15$ 

Flaneuron has abinary sigmoidal function of the form given in Problem 1. It receives four inputs 0.8, 0.3, 0.2, and 0.6 with weights -0.2, 0.3, 0.8 and 0.5, respectively. Find the neuronal output if the weight bias is 0.25.

8] Aneuron has abinary sigmoidal function of the form given in Problem. 1. Derive an expression for the activation, y, in terms of the neuronal output, s. Calculate y for s=0.44.

Inction:  $g(x) = \frac{2}{1 + e^{-x}} - 1$  Verify that: -1 < g(x) = -g(x) and g(-x) = -g(x)Calculate 9(0), 9(2), and 9(-2). Verify that the bipolar sigmoidal function g(x) in Problem. 9, is related to the binary sigmoidal function f(x), in Problem. 1, through the relation  $\mathcal{J}(x) = 2\mathcal{J}(x) - 1$ Represent this relation graphically, what is the value of g(x) when f(x) = 0.5? What is the value of f(x) when g(x) = -1? III verify that the derivative of g(x), in problems, is expressed as:  $\frac{d g(x)}{d x} = \frac{2e^{x}}{(1+e^{x})^{2}} = 0.5 \left[1-g^{2}(x)\right]$ and that it is related to  $\frac{df(x)}{dx}$ , in Phbem 4, as dg(x) = JP(x)as  $\frac{dg(x)}{dx} = 2 \frac{df(x)}{dx}$ sketch the graph of dg(x), referring to its main Properties. Calculate.

$$\frac{dg(x)}{dx}\Big|_{X=2}$$
 and  $\frac{dg(x)}{dx}\Big|_{X=-2}$ 

12) Aneuron has abipolar sigmoidal function of the form given in problem. g. Derive an expression for the activation, y, interms of the neuron al output, s. Calculate y for s = 0.6 and for s = -0.6.

13 Aneuron has an activation y and output's.

Sketch, on the Same s-y coordinate axes, the graphs of y(s), y as a function of s, Ensidering the following two Cases:

a) The neuronal output is of the binary Sigmoidal type, in Problem 1. Verify, in this situation, that y(1-s) = -y(s), 0 < s < 1

b) The neuronal output is of the bipolar Signaidal type, in Problem -9. Verify, in this Situation, that y(-s) = -y(s), -1 < s < 1 (Make use of the expressions derived for y(s) in Problem. 8 and 12).

14] Aneuron has abipolar sigmoidal function of the form given in Problem. 9. It receives three inputs 1.2,2.2, and 1.6 with weights 0.6, 0.8 and 0.7,

respectively. Find the neuronal output if the weight bias is - 1.8.

Aneuron receives four inputs - 2.5, -3.2, -5.1, and 4.4 with weights - 1.5, 1.5, -1.8 and -2.1, respectively. The neuronal output is 0.65. Find the weight bias in each of the following two cases:

a) The neuron has abinary Sigmoidal function of the form given in problem. 1.

b) The neuron has abipolar sigmoidal function of the form given in Problem. 9.

To Consider the neural network illustrated in Fig. 1. Determine the signals si and sz in each of the following two cases:

a) The output neurons have abinary Sigmoidal function of the form given in problem. 1.

b) The output neurons have a bipolar sigmoidal function of the form given in problem. 9.

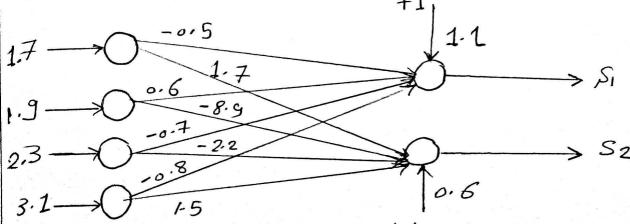


Fig. 1: Neural network for problem. 16.

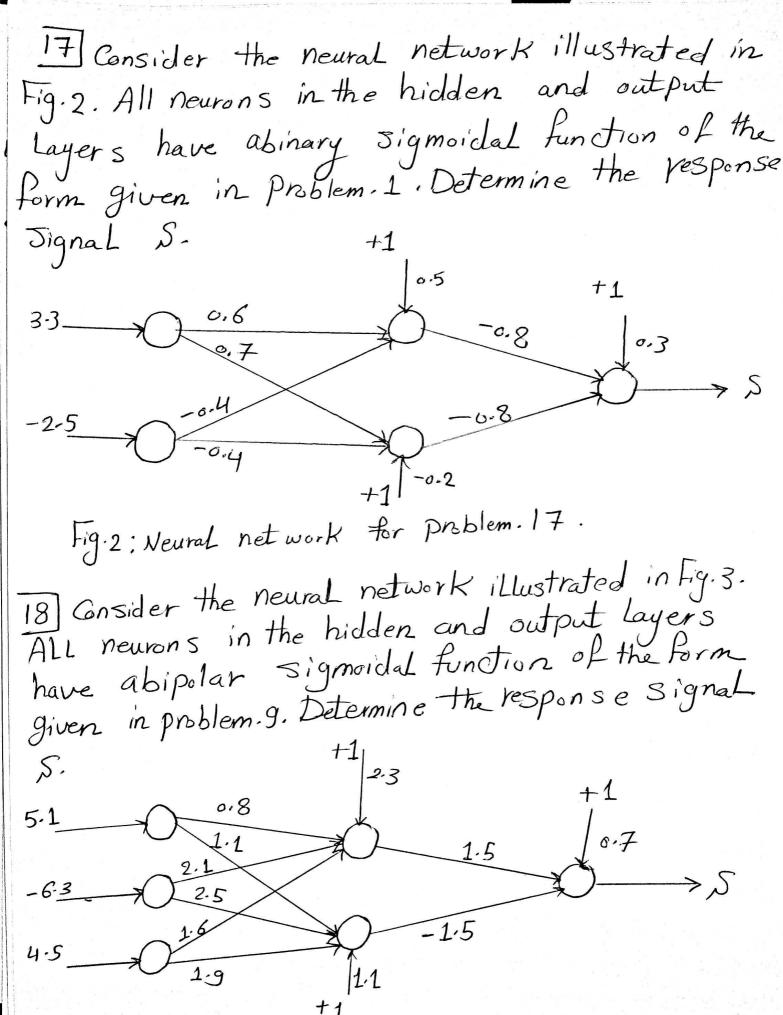


Fig. 3: Neural network for problem. 18.

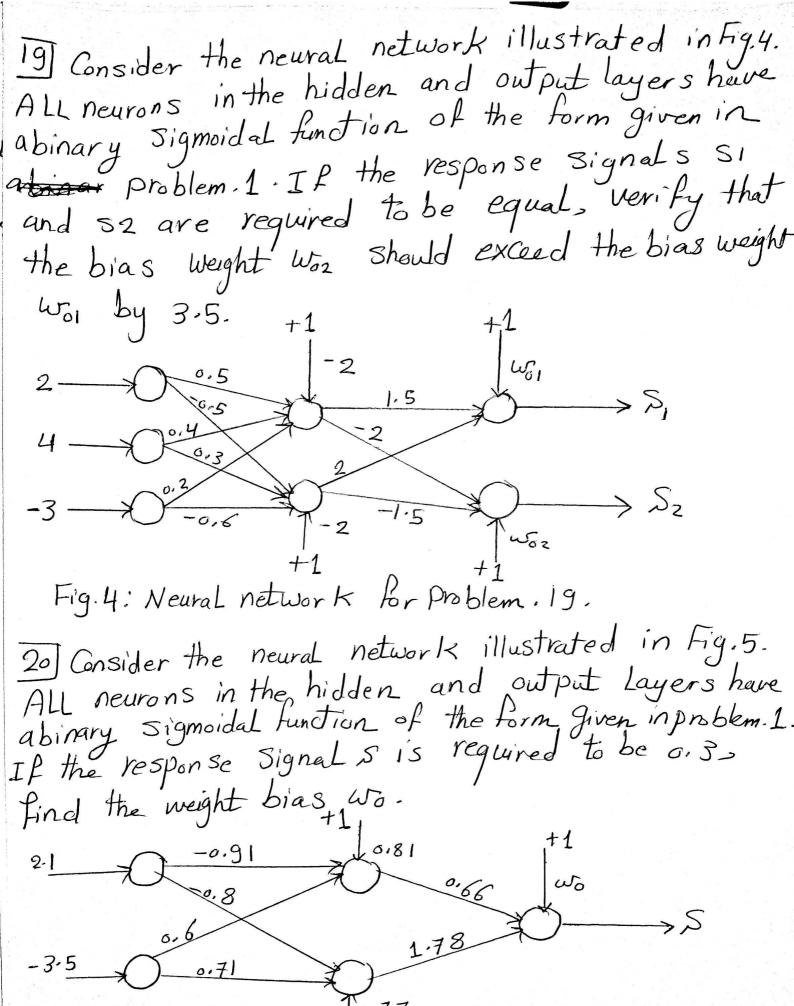


Fig. 5: Neural network for problem. 20.

- In problem 20, if the response 3ignal Sis required to be -0.3, Can you find the Corresponding weight bias wo? Justify.
- In problem 20, let all neurons in the hidden and output layers have abipolar sigmoidal function of the form given in problem. g. Find the weight bias wo when the response signal s is a) 0.3

  b) -0.3
  - In problem 22, if the response signal 5 is required to be 1.5, Can you find the Corresponding weight bias wo? Justify.
  - In aneural network, the input layer has two neurons NI and N2 receiving two inputs \$\alpha\_1=3.2\$ neurons NI and N2 receiving two inputs \$\alpha\_1=3.2\$ neurons NI and NY employing abinary two neurons N3 and NY employing abinary sigmoidal function of the form given in Problem!. The output layer has a single neuron N5 employing abipolar sigmoidal function of the form given in problem. I sigmoidal function of the form given in problem. I the weights (including bias) are:

    Wi3 = 1.5, Wy=-2, W23=-2.2,

    W24 = 3, W35 = 2, W45 = -2,

Was = 1.5, Way = -1.5, Was = 1.5 Determine the response signal, S, of the network.